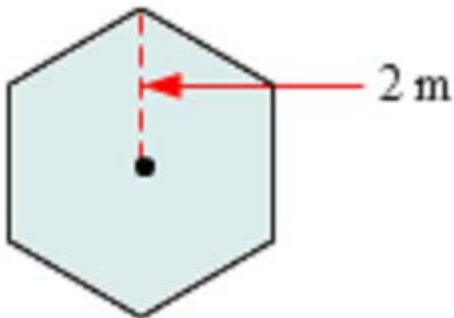
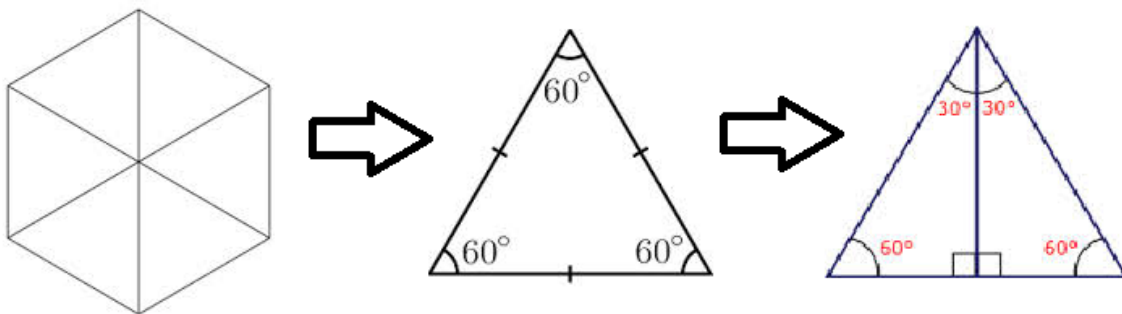


## Find the Area of a Regular Polygon Given the Radius

The question asks for the area of this hexagon. This example has a radius of 2 meters.



We know the hexagon is made up of six equilateral triangles. And each equilateral triangle can be further split in half as a 30-60-90 right triangle.



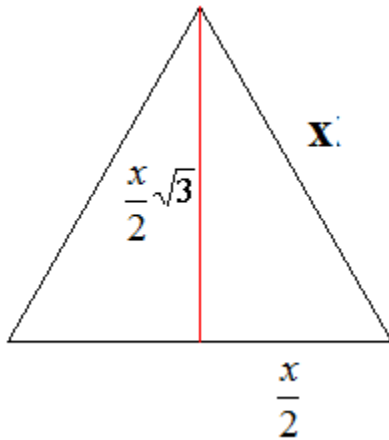
Per the formula, the area is one-half of the apothem times the perimeter.

$$Area = \frac{1}{2}(\text{apothem})(\text{perim})$$

We can easily calculate the perimeter because a side of each triangle is 2 meters. Therefore the perimeter is six times 2 meters or 12 meters: perimeter = 12 meters.

But we still need to calculate the apothem. Remember with 30-60-90 right triangles, the sides have a relationship. The hypotenuse is twice the length of the short side. The longer side is radical three times the short side. See these relationships in the diagram below.

Geometry B Lesson 10.3 Question 1  
Area of a Regular Polygon Given its Radius



The problem gives us that  $x = 2$  meters, which means that for the longer side (which is also the apothem) we can calculate:

$$\text{apothem} = \frac{2}{2}\sqrt{3}$$

$$\text{apothem} = \sqrt{3}$$

Then we substitute the perimeter and the apothem values into the area formula and calculate:

$$\text{Area} = \frac{1}{2}(\text{apothem})(\text{perim})$$

$$\text{Area} = \frac{1}{2}(\sqrt{3})(12)$$

$$\text{Area} \approx 10.4$$